COSMOLOGICAL PARAMETER EXTRACTION FROM THE FIRST SEASON OF OBSERVATIONS WITH DASI

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ABSTRACT

The Degree Angular Scale Interferometer (DASI) has measured the power spectrum of the Cosmic Microwave Background anisotropy over the range of spherical harmonic multipoles 100 < l < 900. We compare this data, in combination with the COBE-DMR results, to a seven dimensional grid of adiabatic CDM models. Adopting the priors h > 0.45 and $0.0 \le \tau_c \le 0.4$, we find that the total density of the Universe $\Omega_{tot} = 1.04 \pm 0.06$, and the spectral index of the initial scalar fluctuations $n_s = 1.01^{+0.08}_{-0.06}$, in accordance with the predictions of inflationary theory. In addition we find that the physical density of baryons $\Omega_b h^2 = 0.022^{+0.004}_{-0.003}$, and the physical density of cold dark matter $\Omega_{cdm} h^2 = 0.14 \pm 0.04$. This value of $\Omega_b h^2$ is consistent with that derived from measurements of the primeval deuterium abundance combined with big bang nucleosynthesis theory. Using the result of the HST Key Project, $h = 0.72 \pm 0.08$, we find that $\Omega_{tot} = 1.00 \pm 0.04$, the matter density $\Omega_m = 0.40 \pm 0.15$, and the vacuum energy density $\Omega_{\Lambda} = 0.60 \pm 0.15$. (All 68% confidence limits.)

Subject headings: CMB, anisotropy, cosmology

1. INTRODUCTION

The angular power spectrum of the cosmic microwave background (CMB) has much to teach us about the nature of the Universe in which we live (Hu, Sugiyama, & Silk 1997). Measurements are improving rapidly (de Bernardis et al. 2000; Hanany et al. 2000; Padin et al. 2001), and for a wide variety of theoretical scenarios the predicted spectra can be calculated accurately (Zaldarriaga & Seljak 2000). Comparison of the data and models allows quantitative constraints to be placed on the parameters of the Universe in which we find ourselves, and is the subject of this paper.

The Degree Angular Scale Interferometer (DASI), along with its sister instrument the CBI (Padin et al. 2001) and the VSA (Jones 1996), is one of several new compact interferometers specifically designed for observations of the CMB. This paper is the third in a set of three. Paper I (Leitch et al. 2001) gives a detailed description of the instrument, observations, and data calibration. Paper II (Halverson et al. 2001) focuses on the extraction of the angular power spectrum from the calibrated interferometric data, and provides band-power estimates of the angular power spectrum of the CMB. In this paper we combine the low-*l* measurements made by the COBE-DMR instrument (Bennett et al. 1996) with the new measurements from DASI to constrain the parameters of cosmological models.

The layout of this paper is as follows. The considerations which drive our selection of the model and parameter space to probe are detailed in §2. In §3 we review the method used to compare band power data to theoretical spectra. The results of this comparison are described in §4, and in §5 we draw some conclusions.

Following the discovery of the CMB, and the realization that the Universe went through a hot plasma epoch, it was proposed that adiabatic density perturbations in that plasma would lead to acoustic oscillations (Peebles & Yu 1970), and a series of harmonic peaks in the angular power spectrum (Doroshkevich, Zeldovich, & Sunyaev 1978). It was assumed that the initial fluctuations were scale invariant only because this is the simplest possible case. It was not until later that (New) Inflation was proposed (Guth & Pi 1982; Bardeen, Steinhardt, & Turner 1983; Hawking 1982; Starobinsky 1982) — an elegant cosmogenic mechanism which naturally produces such conditions. The simplest versions of this theory also make the firm prediction that the Universe is exactly flat, i.e., has zero net spatial curvature.

Although Inflation sets the stage at the beginning of the plasma epoch it has nothing to say about the contents of the Universe. Over the last several decades a wealth of evidence has accumulated for the existence of some form of gravitating matter which does not interact with ordinary baryonic material; the so-called cold dark matter (CDM). Conflicting theoretical expectations and experimental measurements led to the proposal that a third component is present — an intrinsic vacuum energy. This three component model is the scenario we have chosen to consider.

The density required to produce zero net spatial curvature is referred to as the critical density $\rho_c=3H_0^2/(8\pi G)$, where H_0 is the Hubble constant ($H_0\equiv 100h~{\rm km~s^{-1}~Mpc^{-1}}$). It is convenient to measure the present day density of a component of the Universe in units of ρ_c , denoting this Ω_i : the density of baryonic matter Ω_b , the density of CDM Ω_{cdm} , and the equivalent density in vacuum energy Ω_{Λ} . Thus the density of matter is given by $\Omega_m\equiv\Omega_b+\Omega_{cdm}$ and the total density is given by $\Omega_{tot}\equiv\Omega_m+\Omega_{\Lambda}$. Since $\Omega_i=\rho_i/\rho_c$ note that Ω_ih^2 is a physical density independent of the value of the Hubble constant.

To generate theoretical CMB anisotropy power spectra we have used version 3.2 of the freely available CMBFAST program (Zaldarriaga & Seljak 2000). This is the most widely used code of its type, and versions 3 and greater can deal with open, flat and closed universes. CMBFAST calculates how the initial power spectrum of density perturbations is modulated through the acoustic oscillations during the plasma phase, by the effects of recombination, and by reionization as the CMB photons stream through the Universe to the present. The program sets up transfer functions, taking as input Ω_b , Ω_{cdm} and Ω_{Λ} , as well as H_0 , the optical depth due to reionization (τ_c), and some other parameters. It can then translate initial perturbation spectra into the mean angular power spectra of the CMB anisotropy which would be observed in such a universe today. Inflation predicts that the initial spectrum is a simple power law with slope close to, but not exactly, unity.

In any given comparison of data to a multidimensional model we may have external information about the values of some or all of the parameters. This may come from theoretical prejudice, or from other experimental results. It may also be that the data set in hand is unable to simultaneously constrain all of the possible model parameters to the precision which we desire. In such cases we can choose to invoke our external knowledge, and fold additional information about the preferred parameter values into the likelihood distribution. Often this occurs because a parameter which could potentially be free is fixed at a specific value (an implicit prior). Or we may multiply the likelihood distribution by some function which expresses the values of the parameters which we prefer (an explicit prior). The choice of measure, e.g., whether a variable is taken to be linear or logarithmic, is also an implicit prior — although such distinctions become less important as a variable becomes increasingly well constrained.

There is no *a priori* reason to suppose that the marginal likelihoods of the cosmological parameters are Gaussian. Thus the curvature of the likelihood surface at the peak does not fully characterize the distribution. To set accurate constraints it is therefore necessary to explore the complete likelihood space by testing the data against a large grid of models. If the introduction of priors is to be avoided the grid must be expanded until one can be confident that it encompasses essentially all of the total likelihood.

Unfortunately it turns out that even within the paradigm of adiabatic CDM models the anisotropy power spectrum of the CMB does not fully constrain the parameters of the Universe. For example, it is well known that Ω_m and Ω_Λ are highly degenerate. It is always necessary to invoke external information in any constraint-setting analysis. The clear articulation of these priors, both implicit and explicit, is critically important, as has previously been noted (Jaffe et al. 2001).

We have chosen to consider a seven dimensional model space. The parameters which we include are the physical densities of baryonic matter $(\Omega_b h^2 \equiv \omega_b)$ and CDM $(\Omega_{cdm} h^2 \equiv \omega_{cdm})$, as well as the spectral slope of the initial scalar fluctuations (n_s) , and the overall normalization of the power spectrum as measured by the amplitude at the tenth multipole $(C_{10} \equiv l(l+1)C_{10}/2\pi)$. Noting that the degeneracy in the $(\Omega_m, \Omega_\Lambda)$ plane is along a line of constant total density we opt to rotate the basis vectors by 45° and grid over the sum and difference of these parameters: $\Omega_m + \Omega_\Lambda \equiv \Omega_{tot}$ and $\Omega_m - \Omega_\Lambda \equiv \Omega_\Delta$. This reduces the size of the model grid required to box in the region of significant likelihood. The seventh parameter is the opti-

cal depth due to reionization (τ_c) . Note that for each point in $(\Omega_{\Delta}, \Omega_{tot}, \omega_b, \omega_{cdm})$ space there is an implied value of the Hubble constant $(h = \sqrt{2(\omega_b + \omega_{cdm})/(\Omega_{tot} + \Omega_{\Delta})})$ so we can calculate the $(\Omega_b, \Omega_{cdm}, \Omega_{\Lambda}, h)$ values for input to CMBFAST.

We assume, as is the theoretical prejudice, that the contribution of tensor mode perturbations is very small as compared to scalar, and ignore their effect (Lyth 1997). Tensor modes primarily contribute power at low l numbers, so if a large fraction of the power seen by DMR were caused by this effect the scalar spectrum would need to be strongly tilted up to provide the observed power at smaller angular scales. However we know that n_s cannot be $\gg 1$ as this would conflict with results from large scale structure studies. Our constraints should, however, be taken with an understanding of our assumption regarding tensor modes.

In principle some of the dark matter could be in the form of relativistic neutrinos (hot as opposed to cold dark matter). However the change that this would make to the CMB power spectrum is negligible compared to the uncertainties of the DASI data (Dodelson, Gates, & Stebbins 1996). We therefore assume that all the dark matter is cold, and set $\Omega_{\nu}=0$, although it should then be understood that the $\Omega_{cdm}h^2$ value we find may, in principle, contain some hot dark matter.

Papers fitting the BOOMERANG-98 and MAXIMA-1 band-power data (Balbi et al. 2000; Lange et al. 2001; Jaffe et al. 2001) considered seven dimensional grids rather similar to our own. Other studies have examined model grids with as many as 11 dimensions (Tegmark, Zaldarriaga, & Hamilton 2001), including an explicit density in neutrinos and tensor mode perturbations, generally finding both effects to be small.

Taking the philosophy that simplicity is a virtue, we have not made use of l-space or k-space splitting to accelerate the calculation of the model grid (Tegmark et al. 2001). In addition we have generated a simple regular grid, rather than attempting to concentrate the coverage in the maximum likelihood region. Finally we have not treated the normalization parameter C_{10} as continuous, preferring to explicitly grid over this parameter as well. This is computationally somewhat slower, but makes the marginalization simpler, and involves no assumption about the form of the variation of χ^2 versus this parameter. Using the notation lower-edge:step-value:upper-edge (numberof-values) our grid is as follows: $\Omega_{\Delta} = -1.0 : 0.2 : 3.4$ (23), $\Omega_{tot} = 0.7 : 0.05 : 1.3$ (13), $\Omega_b h^2 = 0.0100 : 0.0025 : 0.0400$ (13), $\Omega_{cdm}h^2 = 0.00 : 0.05 : 0.5$ (11), $\tau_c = 0.0 : 0.1 : 0.4$ (5), $n_s = 0.75 : 0.05 : 1.25$ (11), and $C_{10} = 300 : 50 : 1300$ (21). Excluding the small, physically unreasonable corner of parameter space where $\Omega_m \leq 0$, we make 205, 205 runs of CMBFAST generating $205,205 \times 11 = 2,257,255$ theoretical spectra and calculating 2,257,255 × 21 = 47,402,355 values of χ^2 against the data.

For theoretical and phenomenological discussions of how the various peak amplitudes and spacings of the power spectrum are related to the model parameters see Hu et al. (1997) and Hu et al. (2001). In this paper we choose to compare data and models without explicitly considering such connections.

3. COMPARISON OF DATA AND MODELS

Consider a set of observed band-powers \mathcal{D}_i in units of μK^2 , together with their covariance matrix P_{ij} . If the overall fractional calibration uncertainty of the experiment is s we can add this to the covariance matrix as follows:

$$N_{ij} = P_{ij} + s^2 \mathcal{D}_i \mathcal{D}_j. \tag{1}$$

For the purposes of the present analysis we assume s = 0.08which includes both temperature scale and beam uncertainties (the fractional error on the band-powers is 8% corresponding to 4% in temperature units — see Paper II).

Now consider a model power spectrum C_l . The expectation value of the data given the model is obtained through the "bandpower" window function $W_{il}^{\rm B}/l$ (Knox 1999),

$$\mathcal{T}_i = \sum_{l} C_l \frac{W_{il}^{\rm B}}{l}.$$
 (2)

The band-power window functions $W_{il}^{\rm B}/l$ are calculated from the band-power Fisher matrix, F, and the Fisher matrix F^{s} of the bands, b_i , sub-divided into individual multipole moments,

$$\frac{W_{il}^{B}}{l} = \sum_{i'} (F^{-1})_{ii'} \sum_{l' \in b_{i'}} F_{ll'}^{s}, \tag{3}$$

(adapted from Knox 1999, for Fisher matrices with significant off-diagonal elements). The sum of each row of the array $W_{il}^{\rm B}/l$ is unity, so Equation (2) simply represents a set of weighted means. Note that any experiment with less than full sky coverage will always have non top-hat band-power window functions. In practice, we calculate Equation (3) by subdividing each band into four sub-bands, and interpolate the results. The functions for the DASI band-powers are plotted in Figure 1, and are available at our website¹. In practice the effect of using the correct window function, versus simply choosing the C_l at the nominal band center, is extremely modest.

The uncertainties of the \mathcal{D}_i are non-Gaussian so it would not be correct to calculate χ^2 at this point. However it is possible to make a transformation such that the uncertainties become Gaussian to a very good approximation (Bond, Jaffe, & Knox 2000). An additional set of quantities x_i need to be calculated from the data which represent the component of the total uncertainty which is due to instrument noise. We can then transform each of the variables as follows,

$$\mathcal{D}_i^Z = \ln(\mathcal{D}_i + x_i) \tag{4}$$

$$\mathcal{T}_i^Z = \ln(\mathcal{T}_i + x_i) \tag{5}$$

$$M_{ij}^{Z} = N_{ij}^{-1}(\mathcal{D}_{i} + x_{i})(\mathcal{D}_{j} + x_{j}), \tag{6}$$

and calculate
$$\chi^2$$
 as usual,
$$\chi^2 = (\mathcal{D}_i^Z - \mathcal{T}_i^Z) M_{ij}^Z (\mathcal{D}_j^Z - \mathcal{T}_j^Z). \tag{7}$$

The inverse covariance matrix elements M_{ij}^Z will be approximately independent of the bandpowers \mathcal{D}_i . This is true even with the added calibration uncertainty term in Equation (1), under the assumption that the band-power uncertainty is sample variance dominated, i.e., $\mathcal{D}_i/x_i \gg 1$ (as is the case with almost all the DASI band-powers), or that the fractional calibration uncertainty is small compared to the total uncertainty in the bandpower, $s^2 \ll N_{ii}/\mathcal{D}_i^2$, which is the case for DMR. Use of this transformation is very important as it allows us to use χ^2 , and therefore not only to find the best fitting model, but to determine an absolute goodness of fit.

The ability of smaller angular scale (l > 100) CMB data to set constraints on model parameters is much improved when the large angular scale (l < 25) information from the DMR instrument is included. We use the DASI bandpowers described and tabulated in Paper II together with the 24 DMR bandpowers provided in the RADPACK distribution (Knox 2000;

4. RESULTS

Figure 2 shows the DASI band-powers, together with the DMR data condensed to a single point for display. The χ^2 of the best fit model which falls on our grid is 29.5 for the 9 DASI plus 24 DMR band-powers. Assuming a full 7 degrees of freedom are lost to the fit, this is at the 71% point of the cumulative distribution function (cdf)². The parameters of this model are $(\Omega_m, \Omega_\Lambda, \Omega_b h^2, \Omega_{cdm} h^2, \tau_c, n_s, \mathcal{C}_{10}) =$ (0.725, 0.325, 0.0200, 0.15, 0.0, 0.95, 800), equivalent $(\Omega_b, \Omega_{cdm}, \Omega_\Lambda, \tau_c, n_s, h) = (0.09, 0.64, 0.33, 0, 0.95, 0.48)$. However, no particular importance should be ascribed to these the concordance model (Ostriker & Steinhardt 1995; Krauss & Turner 1995) which is shown has a χ^2 of 30.8 (76%) and is also rather a good fit. The message of Figure 2 is simply that there are models within the grid which fit acceptably well, and that we are therefore justified in proceeding to marginalized parameter constraints. We convert χ^2 to likelihood, $\mathcal{L} = e^{-\chi^2/2}$.

The extreme degeneracy of CMB data in the $(\Omega_m, \Omega_\Lambda)$ plane has already been mentioned. This inability to choose between models with the same Ω_{tot} is in fact weakly broken at very low-lnumbers by the Sachs-Wolfe effect (Efstathiou & Bond 1999). The likelihood contours diverge from the $\Omega_{tot} = 1$ line as Ω_{Δ} becomes $\gg 1$, and the allowed region broadens. Consequently the marginal likelihood curve of Ω_{tot} acquires a high side tail as models with progressively greater Ω_{Δ} are included. These high Ω_{Δ} models have very low values of h, and are known to be invalid from a wide range of non-CMB data. This being the case it is clearly not sensible to allow them to influence our results.

We are therefore prompted to introduce additional external information. We could simply restrict Ω_m and Ω_{Λ} to some "reasonable" range; for example requiring $\Omega_{\Lambda} > 0$ and $\Omega_{m} <$ 1. Instead we choose to introduce a prior on h since this strongly breaks the degeneracy and is a quantity which is believed to have been measured to 10% precision (Freedman et al. 2000). We use two h priors; a weak h > 0.45, and a strong $h = 0.72 \pm 0.08$ assuming a Gaussian distribution. For the weak prior adding the additional restriction h < 0.90 has almost no effect as the excluded models already have very small likelihoods. To apply the prior we simply calculate the h value at each grid point, assign it the relevant likelihood, and multiply the two grids together.

Figure 3 shows how the marginal likelihood distributions of the model parameters change as we move from the implicit prior of $(\Omega_{\Delta} \leq 3.4, \Omega_{tot} \leq 1.3)$, to weak, and then strong prior cases. Note that most of the curves fall to a small fraction of their peak value before the edge of the grid is reached. For all parameters where this is not the case one must introduce external priors such that it becomes so, and/or acknowledge the implicit top-hat prior which the range of that grid parameter represents — only then can the constraint on any of the parameters be accepted. All such priors must then be quoted with the constraints. In fact we see that $(\Omega_b h^2, \Omega_{cdm} h^2, n_s, C_{10})$ are

Bond et al. 2000), concatenating the \mathcal{D}_i and x_i vectors and forming a block diagonal covariance matrix. Note that while the effect of the transformation described above is modest for the DASI points, it is very important for those from DMR (due to the large sample variance at the lower l's).

¹ http://astro.uchicago.edu/dasi

² In fact since there is not sufficient freedom in the model that an arbitrary set of 7 band-powers could be fit exactly the effective loss of degrees of freedom is less than 7. For example assuming 4 shifts us to the 56% point of the cdf.

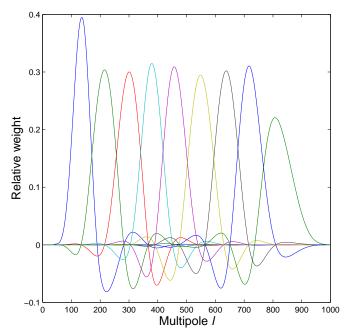


FIG. 1.— Window functions for the DASI band-powers.

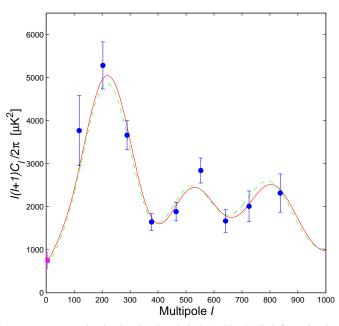


FIG. 2.— The DASI first-season angular power spectrum in nine bands (closed circles). The DMR information is shown compressed to the single lowest l point. The solid (red) line is the best fitting model which falls on our grid, while the dashed (green) shows the concordance model $(\Omega_b, \Omega_{cdm}, \Omega_\Lambda, \tau_c, n_s, h) = (0.05, 0.35, 0.60, 0, 1.00, 0.65)$. The error bars plotted here are strictly for illustrative purposes only. The χ^2 calculation is made using the full covariance matrix, and after the transformation described in §3. Thus "Chi-by-eye" can be misleading.

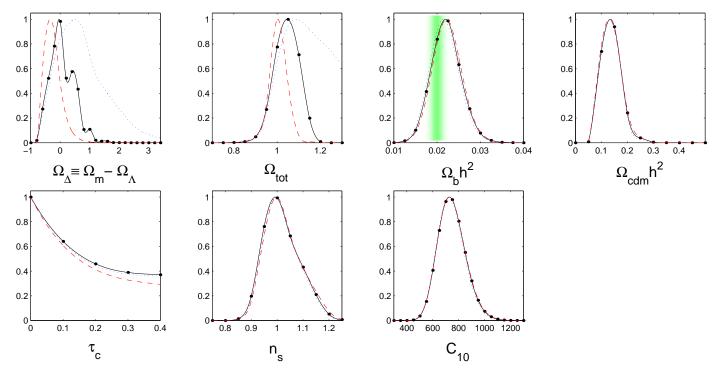


FIG. 3.— Marginal likelihood distributions for each dimension of the model grid. The dotted (blue) and solid (black) lines show the distribution before and after the introduction of a weak prior on the Hubble parameter (h > 0.45). The dashed (red) lines shows the effect of the stronger prior $h = 0.72 \pm 0.08$. In the $\Omega_b h^2$ panel the BBN constraint is shown as a (green) shaded region. All curves are normalized to a peak height of unity, and are spline interpolations of the actual model grid values shown by the points.

almost completely unaffected by the choice of prior on h—this indicates that correlations between these parameters and $(\Omega_{\Delta}, \Omega_{tot})$ are modest, and is a fortunate result.

We turn now to τ_c which, as is evident in Figure 3, is a very poorly constrained parameter. The effect of reionization is to suppress power at small angular scales, and tilt the spectrum down. However this can be compensated by adjusting n_s upwards making these two parameters largely degenerate. Worse still, unlike the h prior discussed above, we have very weak experimental guidance as to the value of τ_c — we know only that reionization occurred at $z \ge 6$, roughly equivalent to $\tau_c \ge 0.03$. From theoretical ideas regarding early structure formation, and energy emission, it seems essentially impossible that $\tau_c > 0.4$ (see Haiman & Knox 1999, for a recent review of our knowledge regarding reionization). The theoretical prejudice for $n_s \approx 1$ is strong, but since this is a fundamental parameter of the cosmology which we are trying to measure, we are very reluctant to place a prior on it.

We have opted to accept the top-hat prior implicit in our model grid, i.e., that the likelihood of τ_c falling between 0.0 and 0.4 is uniform. In Table 1 we list the spline interpolated median, 1σ and 2σ points of the integral constraint curves. The modal (maximum likelihood) value is also given. All of the constraints quoted in this paper are 68% confidence intervals about the median. Although one can argue that the mode is perhaps more natural, in practice it makes little difference.

Referring to Figure 3 we see that the Ω_{Δ} constraint is almost wholly driven by the prior on h; for this reason we have not included it in table 1. However, if one is prepared to accept the strong prior $h=0.72\pm0.08$, then our data indicates that $\Omega_{tot}=1.00\pm0.04$, $\Omega_m=0.40\pm0.15$ and $\Omega_{\Lambda}=0.60\pm0.15$.

Figure 4 illustrates the effect of setting $\tau_c = 0.0$ (which the data weakly prefers). As already mentioned the primary degen-

eracy is with n_s which shifts to $n_s = 0.97^{+0.05}_{-0.04}$.

The selection of the particular set of nine bandpowers which we have used in this analysis is quite arbitrary. We have tested increasing the number of bins — as expected the variance and covariance of the points increases to compensate, and the constraint curves remain the same. Shifting the bins in l also leaves the results unchanged — for instance the alternate binning shown in Paper II leads to results which are indistinguishable from those presented here.

5. CONCLUSION

We have compared the DASI+DMR data to adiabatic CDM models with initial power law perturbation spectra. The best fitting model has an acceptable χ^2 value, indicating that for data of the present quality models within this class are a plausible representation of the underlying physics. Adopting the conservative priors h>0.45 and $0.0\leq\tau_c\leq0.4$, we find $\Omega_{tot}=1.04\pm0.06$ and $n_s=1.01^{+0.08}_{-0.06}$, consistent with the predictions of Inflation. Moving to more aggressive priors on h and τ_c tightens the constraints on Ω_{tot} and n_s respectively but they remain consistent with the theory.

We find that $\Omega_b h^2 = 0.022^{+0.004}_{-0.003}$ and $\Omega_{cdm} h^2 = 0.14 \pm 0.04$, adding to the already very strong evidence for non-baryonic dark matter. These constraints are only weakly affected by the choice of h and τ_c priors. Setting a strong h prior breaks the $(\Omega_m, \Omega_\Lambda)$ degeneracy such that we constrain $\Omega_m = 0.40 \pm 0.15$ and $\Omega_\Lambda = 0.60 \pm 0.15$ — consistent with other recent results.

The current best value for $\Omega_b h^2$ derived from the well developed theory of big bang nucleosynthesis (BBN), combined with measurements of the primeval deuterium abundance, is $\Omega_b h^2 = 0.020 \pm 0.002$ (Burles, Nollett, & Turner 2001, 95% confidence). The χ^2 of the difference between this and our own value is at the 42% point of the cdf (assuming Gaus-

 $\label{eq:table 1} \textbf{Parameter constraints from DASI+DMR data}$

| Parameter | 2.5% | 16% | 50% | 84% | 97.5% | mode |
|--------------------|--------|--------|--------|--------|--------|--------|
| Ω_{tot} | 0.927 | 0.986 | 1.044 | 1.103 | 1.150 | 1.047 |
| $\Omega_b h^2$ | 0.0156 | 0.0187 | 0.0220 | 0.0255 | 0.0292 | 0.0220 |
| $\Omega_{cdm}h^2$ | 0.075 | 0.100 | 0.137 | 0.175 | 0.225 | 0.135 |
| n_s | 0.901 | 0.949 | 1.010 | 1.092 | 1.166 | 0.993 |
| \mathcal{C}_{10} | 558 | 642 | 741 | 852 | 973 | 728 |

These constraints are from a seven dimensional grid, assuming the weak prior h > 0.45, and $0.0 \le \tau_c \le 0.4$. The indicated points on the cumulative distribution function are given, as well as the maximum likelihood value.

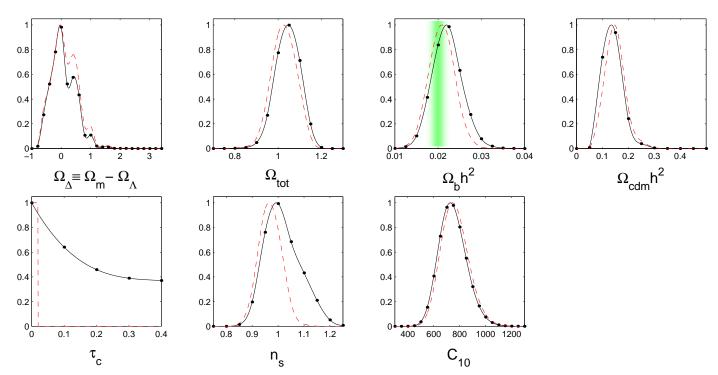


FIG. 4.— Marginal likelihood distributions when varying the prior on τ_c . All curves assume the weak prior h > 0.45. The solid (black) are the same as in Figure 3 and assume $0.0 \le \tau_c \le 0.4$, while the dashed (red) set $\tau_c = 0.0$.

sian errors on both); the values are hence consistent. Previous CMB analyses have seen little power in the second peak region, and have determined $\Omega_b h^2$ values higher than, and inconsistent with, BBN at the $\approx 3\sigma$ level (Lange et al. 2001; Jaffe et al. 2001).

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REFERENCES

Balbi, A., Ade, P., Bock, J., et al., 2000, ApJ, 545, L1, astro-ph/0005124 Bardeen, J. M., Steinhardt, P. J., & Turner, M. S. 1983, Phys. Rev. D, 28, 679 Bennett, C. L., Banday, A. J., Gorski, K. M., et al., 1996, ApJ, 464, L1 Bond, J. R., Jaffe, A. H., & Knox, L. 2000, ApJ, 533, 19, astro-ph/9808264 Burles, S., Nollett, K. M., & Turner, M. S. 2001, Phys. Rev. D, 63, 063512, astro-ph/0008495

de Bernardis, P., Ade, P. A. R., Bock, J. J., et al., 2000, Nature, 404, 955 Dodelson, S., Gates, E., & Stebbins, A. 1996, ApJ, 467, 10, astro-ph/9509147 Doroshkevich, A. G., Zeldovich, I. B., & Sunyaev, R. A. 1978, AZh, 55, 913 Efstathiou, G. & Bond, J. R. 1999, MNRAS, 304, 75 Freedman, W. L., Madore, B. F., Gibson, B. K., et al., 2000, ApJ, 553, 47,

astro-ph/0012376

Guth, A. H. & Pi, S. . 1982, Physical Review Letters, 49, 1110

Haiman, Z. & Knox, L. 1999, in Microwave Foregrounds, ed. A. de Oliveira-Costa & M. Tegmark, Vol. 181 (San Francisco: ASP), 227, astro-ph/9902311 Halverson, N. W., Leitch, E. M., Pryke, C., et al., 2001, ApJ, 568, 38, astro-ph/0104489

Hanany, S., Ade, P., Balbi, A., et al., 2000, ApJ, 545, L5, astro-ph/0005123 Hawking, S. W. 1982, Phys. Lett. B, 115, 295

Hu, W., Fukugita, M., Zaldarriaga, M., et al., 2001, ApJ, 549, 669, astro-ph/0006436

Hu, W., Sugiyama, N., & Silk, J. 1997, Nature, 386, 37, astro-ph/9604166

Jaffe, A. H., Ade, P. A. R., Balbi, A., et al., 2001, Phys. Rev. Lett., 86, 3475,

astro-ph/0007333

Jones, M. E. 1996, in Moriond Astrophysics Meetings, Vol. XVI, Microwave Background Anistropies, ed. B. G. J. V. F.R. Bouchet, R. Gispert (Gif-sur-Yvette: Editions Frontieres), 161, ISBN: 3863322087

Knox, L. 1999, Phys. Rev. D, 60, 103516, astro-ph/9902046 Knox, L. 2000, http://bubba.ucdavis.edu/knox/radpack.html Krauss, L. & Turner, M. S. 1995, Gen. Rel. Grav. 27, 1137, astro-ph/9504003 Lange, A. E., Ade, P. A. R., Bock, J. J., et al., 2001, Phys. Rev. D, 63, 042001,

astro-ph/0005004 Leitch, E. M., Pryke, C., Halverson, N. W., et al., 2001, ApJ, 568, 28, astro-ph/0104488

Astro-ph/0104468 Lyth, D. H. 1997, Phys. Rev. Lett., 78, 1861 Ostriker, J. P. & Steinhardt, P. J. 1995, Nature, 377, 600+, astro-ph/9505066 Padin, S., Cartwright, J. K., Mason, B. S., et al., 2001, ApJ, 549, L1, astro-ph/0012211

Peebles, P. J. E. & Yu, J. T. 1970, ApJ, 162, 815 Starobinsky, A. A. 1982, Phys. Lett., B117, 175

Tegmark, M., Zaldarriaga, M., & Hamilton, A. 2001, Phys. Rev. D, 63, 043007, astro-ph/0008167

Zaldarriaga, M. & Seljak, U. 2000, ApJS, 129, 431, astro-ph/9911219